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A study on physical properties of Coronene oxide as a function of number of oxygen atoms and temperature by density functional theory

Taif Talib Khalaf^a*, and Mohammed T. Hussein b

^aDepartment of Physics, College of Science, University of Baghdad, Baghdad, Iraq ^bAlnukhba University College, Baghdad, Iraq Corresponding author. E-mail: taif.taleb1604a@sc.uobaghdad.edu.iq

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ABSTRACT

The electronic properties like (HOMO, LUMO levels and Energy gap), and spectroscopic properties (IR spectra) in addition to thermodynamics characteristics like (Gibbs free Energy, Enthalpy, Entropy, and Heat capacity) of Coronene C²⁴ and reduced Coronene oxide $C_{24}O_x$ where x=1-5 is a number of oxygen atoms and different temperature from (298 – 398) K were studied. The methodology utilized in this study involved the application of Density Functional Theory (DFT) using the Hybrid functional B3LYP (Becke, 3 parameters, Lee -Yang-Parr) with 6-311G** basis sets. The band gap of Coronene (C24) 3.5 eV was calculated, while for reduced coronene oxide $C_{24}O$ - $C_{24}O_5$ has been varied from (1.68 to 0.89) eV due to broken symmetry and adding levels inside the energy gap. The IR intensity of $C_{24}O_5$ increases with increasing temperature between (298 and 398) K because of the number of excited atoms, the spectroscopic properties were compared with experimental results, in particular the Longitudinal Optical (LO) mode of vibration for graphene oxide 1582 cm-1 which agreed well. The Gibbs free energy and enthalpy decreased (in the negative sign) with an increased number of oxygen atoms and temperatures which means an exergonic reaction.

Keywords: *Coronene oxide, Electronic, Spectroscopic, Thermodynamics properties, DFT*

1. INTRODUCTION

Coronene, a polyaromatic hydrocarbon (PAH) molecule characterized by a core ring shared with six surrounding rings, is recognized as a distinctive super benzene molecule. It is naturally present in sedimentary rock and can also be detected during the hydrocracking process in petroleum refining $[1-5]$. The sp² carbon structure has garnered significant attention in the synthesis of several πconjugated organic compounds [6-10]. And further electronic [11]. Coronene is classified as a polycyclic aromatic hydrocarbon (PAH) because of its molecular structure, which consists of six benzene rings that are fused together in a peri arrangement. This unique arrangement allows for the electrons within Coronene to be completely delocalized among the benzene rings. Their unique planar electrical structure allows Coronene molecules to tightly stack, which promotes efficient self-assembly and increased electron mobility [12-17]. Carbon nanotubes and graphene, two materials with remarkable electron conductivity, are thought to represent extensions of the Coronene structure. Several attempts have been made to create Coronene derivatives with a variety of electrical and electronic characteristics [18-24]. The first use of graphene was in the field of electronic devices, focusing on its electronic properties [25-27]. Graphene has been applied in numerous fields, such as energy storage devices like lithium-ion batteries, supercapacitors, gas detection and conducting electrodes [28-30]. Previous studies used Coronene (C24H12) as a model to analyze spectroscopic and structural

changes in graphene oxide (GO) due to oxygenated groups. Geometry optimization, vibrational IR, and Raman spectra of functionalized Coronene molecules are performed. The results provide valuable data for GO IR and Raman spectra analysis, revealing more detailed structural effects [31]. Studied analysed the molecular structure of Coronene and Coronene-Y molecules using geometrical optimization. It was found that Y atoms interacting with Coronene resulted in new bonds and reduced ionization potential but increased electron affinity. Coronene acted as a donor in Coronene-Y, while Coronene-B and C had an energy gap similar to semiconductors. Coronene-In was the most polarizable molecule, while Coronene-C and Coronene-O were anti-ferromagnetic [32]. Benzene, Coronene, and Circumcoronene of graphene quantum dots (GQDs) with zigzag edges were studied, utilizing the DFT theory and PBE functional, this study examines the alteration of individual properties about the quantity of atoms present in the graphene quantum dots (GQDs), while also noticing both linear and nonlinear fluctuations. This work additionally examines the utilization of Raman spectroscopy in the context of comparing the PBE and B3LYP functional for various sizes of graphene quantum dots (GQDs). Furthermore, the investigation explores the changes observed in the G peak for each function. The calculations were conducted using the Gaussian 09W software tool, employing 3-21G Gaussian basis sets. The results of this study have substantial implications in several disciplines, Khalaf et al. / A Study on physical properties of Coronene oxide as a function of number of oxygen atoms and temperature by density functional theory

such as materials science and the field of energy storage [33]. In our previous study the electronic properties of Coronene (C_{24}) , reduced Coronene oxide $(C_{24}O_5)$ and the interaction between $C_{24}O_5$ and nitrogen dioxide using DFT, and Gaussian view 05 software [34]. Also the electronic characteristics such as band gap HOMO and LUMO level, as well as the spectroscopic properties like IR and Raman spectra of Coronene C24H¹² after removing hydrogen atoms and substituting with oxygen to get reduced Coronene oxide $(C_{24}O - C_{24}O₅)$, were studied [35]. In the present work adds the variation of temperature as well as the number of oxygen atoms to give a complete aspect of the electronic, spectroscopic and thermodynamic properties of Coronene C_{24} and Reduced Coronene Oxide $C_{24}O_X$ where x=1-5 which is a very important Nanostructure in optoelectronics devices.

2. METHODOLOGY

The DFT is the most dependable technique for comprehending the characteristics and structure of molecules and nanostructures. DFT has gained a reputation because of its strong match to experimental data. Among the most often used DFT methods is B3LYP [36-41]. It was discovered that the B3LYP was better than other functional that encouraged its utilization. Energy from exchangecorrelation sources is combined with HF exchange in the hybrid functional B3LYP [42]. For light atoms such as C and O, we will adopt 6-311G** basic states in this investigation [43, 44]. In order to account for the frequency of vibration, scaling factors with a value of 0.967 were employed [45]. The geometric analysis was carried out using Gaussian view 05, while the computations were carried out using Gaussian 09W software [46] as shown in Figure 1.

3. RESULTS AND DISCUSSION

3.1. Electronic Properties

The energy gap, also known as the band gap, refers to the change in energy levels between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO) [47].

$$
Eg = |LUMO - HOMO| \tag{1}
$$

The energy gap (Eg) can be found from differences between the first low unoccupied molecular orbital (LUMO) which is similar to the conduction band (C.B) and the last high occupied molecular orbital (HOMO) which is equal to the valance band (V.B) of Coronene (C_{24}) and reduced coronene oxide ($C₂₄O_X$) where (X=1-5) as a function of a number of oxygen atoms as shown in Figure 2 which shows the energy levels (HOMO and LUMO). Figure 3 The energy gap of Coronene C²⁴ and reduced coronene oxide C24O-C24O⁵ with fluctuations because of the small number of atoms which are within the computer capabilities compared with the experimental value (1.4) eV for Graphene [48] and a range of (1-2.2) eV for graphene oxide (GO) [49, 50].

The energy band gap of Coronene (C_{24}) is determined to be 3.5 eV, primarily attributed to the strong symmetry of the Coronene nanostructure. The band gap of quasiparticles is significantly influenced by both the Coulomb interaction and the quantum confinement geometry [51]. There was a decrease in the energy gap with an increase in the number of oxygen atoms adding to a Coronene (C_{24}) because of the symmetry broken and adding level inside of the energy gap.

Figure 1. Geometrical optimization of (a) Coronene C₂₄ and (b, c, d, e, f) reduced Coronene oxide (C₂₄O - C₂₄O₅)

Figure 2. Energy levels (HOMO and LUMO) of Coronene C²⁴ and reduced Coronene oxide (C24O - C24O5) as a function of a number of oxygen atoms

3.2. Thermodynamics Properties

Figure 4 and Table 1 show the variation of the Gibbs free energy (∆G), Enthalpy (∆H), Entropy (∆S) and Heat capacity (CV) with a number of oxygen atoms at room temperature 298 K. Figure 5 and Table 2 shows the thermodynamics properties at different temperature from (298-398) K for Coronene C_{24} and reduced coronene oxide $C_{24}O$ - $C_{24}O_5$. It has been found that when the number of oxygen atoms increases, the system size increases and interaction between the atoms causes Gibbs free energy and enthalpy to decrease (negative sign), while with the increased temperature that ∆G decreased according to the Eq. (2), which indicate an exergonic reaction. Both the heat capacity and entropy increase with the number of oxygen atoms and

Figure 3. The energy gap of Coronene C²⁴ and reduced Coronene oxide $(C_{24}O - C_{24}O_5)$ according to the oxygen atoms

temperature; this results in greater disorder within the system and a higher material temperature, as shown in the following Eqs. (2) and (3) [52,53]:

$$
\Delta G = \Delta H - \Delta ST \tag{2}
$$

where, ΔH is change in the enthalpy and ΔS is change in the entropy.

$$
C = Q/m\Delta T \tag{3}
$$

where C is heat capacity $(J/(kg·K), Q)$ is the amount of heat (in joules), m is the mass of the sample, and ΔT is the change between starting and end temperatures.

Figure 4. The thermodynamics properties of reduced Coronene oxide (C₂₄O-C₂₄O₅) compare with Coronene C₂₄ for (a) Gibbs free energy, (b) Enthalpy, (c) Entropy and (d) Heat capacity of a number of oxygen atoms

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Figure 5. The thermodynamics properties of reduced Coronene oxide (C₂₄O₅) for (a) Gibbs free energy, (b) enthalpy, (c) entropy and (d) heat capacity at different temperatures

Table 1. The thermodynamics properties of C₂₄ and C₂₄O-C₂₄O₅

Thermodynamics properties	C24	C_{24} O	$C_{24}O_2$	$C_{24}O_3$	$C_{24}O_4$	$C_{24}O_5$
ΔG (a.u)	-913.97	-989.20	-1064.41	-1139.62	-1214.85	-1290.07
ΔH (a.u)	-913.92	-989.14	-1064.35	-1139.55	-1214.79	-1290
ΔS (Cal/Mol-K)	117.25	122.91	127.76	133.57	138.86	143.20
CV (Cal/Mol-K)	61.92	65.25	68.74	72.74	76.20	79.19

3.3. Spectroscopic Properties

Figure 6 and Table 3 illustrate how the intensity of the IR absorption spectra of reduced coronene oxide $(C_{24}O_5)$ increases with temperature between (298 and 398) K because of an increase in the number of excited atoms according to Maxwell Boltzmann distribution, comparison with the experimental value of Longitudinal optical (LO) mode of frequency 1582 cm-1 for graphene oxide [54].

4. CONCLUSIONS

Density functional theory with Hybrid functional B3LYP and 6-311G** basis sets were used to study the Coronene molecule with a variation of the number of oxygen atoms and the temperature. The obtained results can be summarized as follows.

- 1. The energy gap of the Coronene molecule was high because of the quantum confinement effect and Coulomb interaction.
- 2. It was found that the energy gap decreased with the substituting of oxygen atoms instead of hydrogen of Coronene molecule due to broken symmetry and adding level inside of the energy gap.
- 3. The Gibbs free energy decreased (in the negative sign) with an increase of oxygen atoms and variation of the temperature which means exergonic reaction with more stable as the definition of Gibbs free energy requires.
- 4. The intensity of the IR absorption spectrum of $C_{24}O_5$ was increased with increased temperature due to an increase in the number of excited atoms according to Maxwell Boltzmann distribution.

Figure 6. IR spectra for reduced Coronene oxide C₂₄O₅ as a function of frequency for (a) at 298 K and (b) at 398 k

Table 3. The IR intensity and frequency values of $C_{24}O_5$ at different temperatures (298 and 398) K

Temperature (k)	IR Intensity (a.u)	Theoretical Frequency cm^{-1}	Experimental Frequency (cm- [54]
298	3264.46	1695	1582
398	4549.22	1695	1582

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